§*5.1 Area and Estimating with Finite Sums*

A. **Problem.** Estimate the area under the graph of $f(x) = 20 - x^2$ on $0 \le x \le 4$ using
(a) left-endpoint values with two rectangles of equal width.
(b) left-endpoint values with four rectangles of equal width.
(c) right-endpoint values with two rectangles of equal width.
(d) right-endpoint values with four rectangles of equal width.

Exercise 10. You are sitting on the bank of a tidal river watching the incoming tide carry a bottle upstream. You record the velocity of the flow every 5 minutes for half an hour, with the results shown in the accompanying table.

Time (min)	0	5	10	15	20	25	30
Velocity (m/sec)	1	1.2	1.7	2.0	1.8	1.6	1.4

About how far upstream did the bottle travel during those 30 minutes? Find an estimate using 6 subintervals of length 5 with
(a) left-endpoint values.
(b) right-endpoint values.

B*. Recitation Session: Project on evaluate area under a curve using finite Riemann sums

C. [Ex. from MML]

D. Video on The Area Under a Curve (28 minutes)